

quiz 6: 9:00AM

① $y^{(4)} - 6y'' + 11y' - 6y = 0$

\Rightarrow characteristic polynomial

$$r^3 - 6r^2 + 11r - 6 = 0$$

$r=3$ is one root:

$$(r^3 - 6r^2 + 11r - 6) : (r - 3) = r^2 - 3r + 2$$

$$\begin{array}{r} -r^3 + 3r^2 \\ \hline \end{array}$$

$$0 \quad -3r^2 + 11r$$

$$\quad +3r^2 - 9r$$

$$\begin{array}{r} 0 \quad 2r - 6 \\ \hline \end{array}$$

$$\quad -2r + 6$$

$$\quad \quad \quad 0$$

$$\Rightarrow (r^3 - 6r^2 + 11r - 6) = (r - 3)(r^2 - 3r + 2)$$

roots of $r^2 - 3r + 2 = 0$

$$r = \frac{3}{2} \pm \sqrt{\frac{9}{4} - 2} = \frac{3}{2} \pm \frac{1}{2} = 2, 1$$

$$\Rightarrow (r^3 - 6r^2 + 11r - 6) = (r - 3)(r - 1)(r - 2)$$

\Rightarrow general sol. to given eq. (1):

$$\underline{\underline{y(t) = c_1 e^{3t} + c_2 e^{2t} + c_3 e^t, \quad c_1, c_2, c_3 \in \mathbb{R}.}}$$

2.)

$$\frac{1}{(s-1)^2} + \frac{s-1}{s^2-2s+5} = \mathcal{L}(\text{?})$$

$$\rightarrow \frac{1}{(s-1)^2} = \frac{d}{ds} \left(\underbrace{\frac{1}{(s-1)} \cdot (-1)}_{\mathcal{L}(-e^t)} \right) = \mathcal{L}(te^t)$$

$$\rightarrow \frac{s-1}{s^2-2s+5} = \frac{(s-1)}{(s-1)^2+4} = \mathcal{L}(\cos(2t)e^t)$$

$$\Rightarrow \frac{1}{(s-1)^2} + \frac{s-1}{s^2-2s+5} = \underline{\underline{\mathcal{L}(te^t + \cos(2t)e^t)}}$$