

$$2.) \quad y'(x) = (1+x)(1+y^2)$$

$$\frac{y'(x)}{1+y^2} = (1+x)$$

$$\Rightarrow \arctan(y) = x + \frac{x^2}{2} + C$$

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5:00 PM - solutions

$$1.) \quad \begin{cases} y'(t) = t(y^2 - t \cos t) \\ y(\frac{\pi}{2}) = 0 \end{cases}$$

(i) order = 1

linear, inhomogeneous deg.

(ii) homog. eq. (gen. sol.):

$$y_h'' - t y_h' = 0$$

$$\frac{y_h'}{y_h} = \frac{1}{t}$$

$$\ln |y_h| = \ln |t| + D$$

$$\Rightarrow y_h(t) = Ct, \quad C \in \mathbb{R}$$

inhomog. eqn. (variation of constant):

$$y(t) = C(t)t$$

$$\Rightarrow \cancel{C(t)t} - t(C'(t)t + \cancel{C(t)}) = -t^2 \cos t$$

$$-t^2 C'(t) = -t^2 \cos t$$

$$C'(t) = \cos t$$

$$\text{since } 0 = y(\frac{\pi}{2}) = C(\frac{\pi}{2}) \frac{\pi}{2}$$

$$\Rightarrow C(\frac{\pi}{2}) = 0$$

$$\Rightarrow C(t) = (\sin t - 1) \Rightarrow \underline{\underline{y(t) = (\sin t - 1)t}}$$